System-level simulation of a solar power tower plant with thermocline thermal energy storage

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Highlights

- Molten-salt thermocline tanks offer low-cost thermal energy storage for concentrating solar power plants.
- A new thermocline tank model is developed to provide comprehensive thermal simulation at low computational cost.
- The thermocline model is incorporated into a system model to study storage performance over long-term plant operation.
- Yearlong simulation of a power tower plant indicates excellent storage performance with the thermocline tank concept.

Abstract

A thermocline tank is a low-cost thermal energy storage subsystem for concentrating solar power plants that typically utilizes molten salt and quartzite rock as storage media. Long-term thermal stability of the storage concept remains a design concern. A new model is developed to provide comprehensive simulation of thermocline tank operation at low computational cost, addressing deficiencies with previous models in the literature. The proposed model is then incorporated into a system-level model of a 100 MWe power tower plant to investigate storage performance during long-term operation. Solar irradiance data, taken from measurements for the year 1977 near Barstow, CA, are used as inputs to the simulation. The heliostat field and solar receiver are designed with DELSOL, while the transient receiver performance is simulated with SOLERGY. A meteorological year of plant simulation with a 6-h capacity for the thermocline tank storage yields an annual plant capacity factor of 0.531. The effectiveness of the thermocline tank at storing and delivering heat is sustained above 99% throughout the year, indicating that thermal stratification inside the tank is successfully maintained under realistic operating conditions. Despite its good thermal performance, structural stability of the thermocline tank remains a concern due to the large thermal expansion of the internal quartzite rock at elevated molten-salt temperatures, and requires further investigation.

1. Introduction

Concentrating solar power (CSP) exploits the conversion of direct sunlight to high-temperature heat for large-scale power production. While it is a sustainable and environmentally benign source of energy, sunlight is an intermittent resource whose intensity is subject to planetary rotation, orbit, and atmospheric effects associated with weather conditions. Commercial facilities must therefore decouple solar collection from power production to meet consumer demand, independent of the prevailing conditions of solar irradiance. The generation of high-temperature heat in CSP plants provides built-in potential for the use of thermal energy storage systems to achieve this decoupling. While several design concepts exist for thermal energy storage, commercial storage systems must exhibit low cost, reliability, and effective delivery of heat for power production.

Thermal storage mechanisms involve sensible heat, latent heat, or thermochemical reactions. Sensible heat-based systems offer low energy densities but enable direct integration into the solar collection flow loop, avoiding rate-limiting steps inherent to the alternative phase-change or reaction-based approaches. Application of sensible storage is also practical for traditional Rankine cycles, where heat addition to the working fluid occurs across a temperature rise. Current CSP plants featuring thermal energy storage therefore apply a sensible heat-based concept known as two-tank storage. In the case of a power tower plant employing this storage system, hot fluid (e.g., molten salt) exits the solar receiver during daylight and flows to a nominally isothermal hot tank. When power...
production is subsequently desired under no-sunlight conditions, salt is extracted from this tank and sent to the plant power block for steam generation. While this system is simple and effective, mass balance in the collection loop requires a second tank upstream of the solar receiver to store the excess cold salt exiting the power block. This cold tank adds to the plant cost without providing any energy benefits.

The two-tank concept can be modified to save cost by storing the excess hot and cold molten salt inside a single tank volume, removing the physical redundancy of a second tank. Separation of the hot and cold fluid is retained in this thermoline tank via fluid buoyancy forces that help stratify the two isothermal regions along the vertical direction. At the interface of the hot and cold fluid, an intermediate layer of high temperature gradient develops, known as the thermoline or heat-exchange region. This sigmoid-shaped stratification is sustained over repeated storage cycles that involve flow reversal of the internal molten salt. During operation, the tank is energized or charged with hot salt entering at the top of the tank while cold salt is pumped out from the bottom. The heat-exchange region between the hot and cold salt travels downward as the hot salt is removed from the top of the tank. Additionally, the tank can be equipped with storage tanks, allowing for system expansion during periods of low power demand.

A 170 MW hot salt thermoline tank was installed at the historic Solar One pilot plant in Daggett, CA [2]. The tank operated from 1982 to 1986 and was filled with Caloria HT-43 mineral oil and granite rock. The use of mineral oil as the heat transfer fluid limited the storage system to a maximum temperature of 304 °C, a temperature suitable only for auxiliary steam generation. However, the thermoline tank satisfied its original design objectives. Sandia National Laboratories later constructed a small 2.3 MW hot salt tank to validate the thermoline concept with molten salt and quartzite rock filler [1]. The concept was again determined to be a valid and feasible addition to solar power plants with a projected cost savings of 33% compared to the baseline two-tank storage design.

The elevated temperature and large physical scale of the thermoline tank have limited a majority of investigations to numerical analysis. A multidimensional computational fluid dynamics (CFD) model was developed by Yang and Garimella [3] to simulate mass, momentum, and energy transport inside a molten-salt thermoline tank. A two-temperature model resolved energy transport in both the molten-salt and solid filler regions. The governing conservation equations were discretized with the finite-volume method and solved with FLUENT, a commercial CFD package. With this model, the authors investigated thermoline performance during discharge with several different tank geometries and discharge powers. Well-insulated tanks exhibited improved performance at low Reynolds numbers and increased tank heights. For non-adiabatic tanks with significant external heat losses, discharge performance instead improved with increasing Reynolds number, due to the decreased fluid residence time inside the tank and reduced exposure to the heat loss condition [4]. Xu et al. [5] later modified the adiabatic model to perform a sensitivity study of material properties on storage performance. Flueckiger et al. [6] extended the non-adiabatic model to investigate thermal ratcheting phenomena in the thermoline tank wall.
Van Lew et al. [7] modeled energy transport inside a thermocline tank with the one-dimensional Schumann equations. Corresponding analysis of the mass transport was omitted by assuming constant fluid density and velocity. A solution to the energy equations was obtained with the method of characteristics and required minimal computational times. For cyclic tank operation, the authors reported improved performance with reduced filler size and increased fluid velocity, and attributed these findings to the improved convective heat transfer between the fluid and rock. The authors also reported that axial heat conduction was negligible during tank operation, but omitted analysis of the standby periods between the charging and discharging processes when fluid in the tank is stagnant.

Kolb [8] developed a system-level model of the 50 MWt Anda-sol parabolic trough plant in TRNSYS to simulate and compare annual plant output between two-tank and thermocline storage systems. Simulation of the thermocline tank was limited to energy transport with a standard TRNSYS component, but modified to include thermal diffusion and external heat losses. The annual plant output with thermocline tank storage was reported to be near equivalent to the two-tank plant. However, this similarity was contingent on sliding-pressure operation in the power block, which is necessary to accommodate molten salt exiting the thermocline tank below the hot temperature limit.

Comparison of the various thermocline tank simulations in the literature illustrates a persistent tradeoff between detailed CFD models with high computing cost and simplified energy transport models with low computing cost. In the current study, the authors seek to eliminate this tradeoff with a new thermocline tank model that is both comprehensive and computationally inexpensive. Development of the proposed model and subsequent validation with experimental data is discussed in the next section. Thermocline tank performance is then investigated at a system level with a commercial-scale CSP plant model, informed by recorded sunlight data and real plant operating conditions. While system-level studies with thermocline tank storage were previously reported by Kolb [8], his analysis was limited to synthetic oil parabolic trough plants with indirect storage. The current study instead investigates a 100 MWt power tower plant with molten-salt heat transfer fluid and direct integration of the thermocline tank within the solar collection loop. Discussion of the corresponding solar collector and power block models is included in later sections. The integrated plant model is subjected to an entire meteorological year of sunlight data measured near Barstow, CA in 1977. Plant capacity factor and storage effectiveness are monitored throughout the year to quantify the contribution of the storage system to power production as well as the long-term sustainment of vertical thermal stratification inside the thermocline tank.

2. Thermocline tank model development

A schematic diagram of the thermocline tank concept is illustrated in Fig. 1. The tank is operated with a commercial molten nitrate salt mixture (60 wt% NaNO₃, 40 wt% KNO₃) as the heat transfer fluid. The salt is liquid above 220 °C; however, the enforced operating range is 300–600 °C to avoid inadvertent salt freezing in the plant infrastructure. This temperature span exceeds that of current power tower plants, which operate between 290 °C and 565 °C, but is assumed to be achievable through advancements in solar receiver performance. Physical properties of the salt in the liquid phase are known functions of temperature (degrees Celsius) [9,10]:

\[
\rho_l = 2090 - 0.6367T_i \quad (1)
\]

\[
k_l = 0.443 + 1.9 \times 10^{-4}T_i \quad (2)
\]

The specific heat of the molten salt is relatively constant with temperature and is approximated to have a constant value of 1520 J/kg-K. Over the operating temperature span, this value exhibits a maximum deviation of 1.7% versus reported data [10]. For the quartzite rock filler, density, specific heat, and thermal conductivity are all assumed constant: 2500 kg/m³, 830 J/kg-K, and 5 W/m-K, respectively [3,11]. The porosity of the quartzite rock bed is fixed at 0.22 based on past experimental observation [1].

Given the inherent molten-salt density variation with temperature, a thermocline tank cannot be treated as a control volume. The liquid level inside the tank rises when the tank is filled with hot salt and falls when the tank is filled with cold salt. Therefore, an additional volume of molten salt must be maintained above the quartzite rock to prevent dryout of the porous region. Past thermocline studies in the literature have neglected the inclusion and influence of this "liquid heel" in order to achieve a tacit control volume condition for numerical simulation. In contrast, the current study includes simulation of both the porous region and the liquid heel, as discussed in the following sections.

2.1. Porous region

Fluid and solid energy transport in the porous region are governed by the following conservation equations:

\[
\frac{\partial (\rho_l C_p(T_i - T_s))}{\partial t} + \nabla \cdot (\rho_l C_p(T_i - T_s)) = \nabla \cdot (k_l \nabla T_i) + h_i(T_s - T_i) \quad (4)
\]

\[
\frac{\partial ((1 - \varepsilon)\rho_s C_{ps}(T_s - T_2))}{\partial t} = -h_i(T_s - T_i) \quad (5)
\]

Spatial discretization of the filler region is neglected as the temperature in each solid rock is assumed to be homogeneous. Thermal diffusion between the solid filler rocks is also assumed to be negligible due to inter-particle contact resistance. However, the thermal conductivity of the rock does influence thermal diffusion in the fluid region, and is represented with an effective thermal conductivity. This effective value is calculated with the Gonzo correlation [12]:

![Fig. 1. Schematic illustration of a molten-salt thermocline tank, including the porous quartzite rock bed and the liquid heel. Hot salt is supplied at the liquid heel through the top manifold and is extracted via the hot pump. Cold salt enters the porous bed through the bottom manifold but is also extracted through the manifold via the cold pump.](image-url)
\[ k_{\text{eff}} = k_1 \left( 1 + 2\beta \epsilon + (2\beta^2 - 0.1\beta)\epsilon^2 + \phi^2 \exp(4.5\rho) \right) \frac{1}{1 - \beta \epsilon} \]  

(6)

where \( \phi = 1 - \epsilon \) and \( \beta = (k_1 - k_0)/(k_1 + 2k_0) \). Eqs. (4) and (5) are also coupled by interstitial forced convection between the molten salt and quartzite rock. This convection coefficient is calculated with the Wakao and Kaguei correlation [13]:

\[ \text{Nu}_l = 6(1 - \epsilon)[2 + 1.1 \text{Re}^{0.6} \text{Pr}^{1/3}] \]  

(7)

The length scale used in the definition of Reynolds number is the effective diameter of the granulated rock.

For simplification, the thermocline tank is assumed to be well-insulated and to experience laminar and plug flow throughout the fill bed (i.e., any maldistribution of molten salt entering from the tubing manifolds is negligible). As a result, Eq. (4) reduces to a one-dimensional formulation along the axial direction. The molten-salt tubing manifolds is negligible). As a result, Eq. (4) reduces to a one-dimensional formulation along the axial direction. The molten-salt and solid filler temperatures are also normalized with respect to the hot and cold temperature limits:

\[ \Theta = \frac{T - T_s}{T_h - T_c} \]  

(8)

Energy transport in the porous region reduces to the following differential equations:

\[ \frac{\partial (\rho C_p \Theta)}{\partial t} + \frac{\partial (\rho u C_p \Theta)}{\partial x} = \frac{\partial}{\partial x} \left( k_0 \frac{\partial \Theta}{\partial x} \right) + h_i(\Theta_t - \Theta_i) \]  

(9)

\[ \frac{\partial [(1 - \epsilon) \rho C_p \Theta_i]}{\partial t} = -h_i(\Theta_t - \Theta_i) \]  

(10)

As previously discussed, all material properties are either constant or known functions of temperature. The remaining variables include the fluid and solid temperatures as well as the fluid velocity \( u \) in the convection term of Eq. (9). With two equations and three unknowns, an additional relationship is needed to obtain a unique temperature solution. Yang and Garimella [3] previously reported an inherent relationship between the speed of the heat-exchange region and the velocity of the molten salt entering the fill bed:

\[ v = \frac{\rho \epsilon u_{\text{in}} C_p^f}{\rho \epsilon u_{\text{in}} C_p^f + (1 - \epsilon) \rho C_p s u_{\text{in}}} \]  

(11)

However, this relationship between fluid velocity and the resulting vertical shift of the heat-exchange region is not limited to the porous-bed inlet and can be reformulated for any bed location where molten-salt density and velocity are known. Eq. (11) is combined with an alternative formulation at an arbitrary axial location inside the bed to yield the following:

\[ u_x = \frac{\rho \epsilon u_{\text{in}} C_p^f + (1 - \epsilon) \rho C_p s}{\rho \epsilon u_{\text{in}} C_p^f + (1 - \epsilon) \rho C_p s + \rho \epsilon u_{\text{in}}} \]  

(12)

Eq. (12) reveals an inherent relationship between the fluid density field and the velocity field inside the porous bed, independent of time. Thus the thermocline fluid velocity can be determined throughout the porous bed without an explicit calculation of mass or momentum conservation.

Solution to the reduced-order energy transport model in the porous bed region is obtained via a finite-volume method. The transient term is discretized with a first-order implicit method. Spatial discretization of the convective flux term is accomplished with the quadratic flux limiter, a quasi-second-order local extrema diminishing scheme. Picard iteration is implemented to resolve the non-linearity in Eq. (9) as well as the interstitial convection coupling with Eq. (10). The resultant algebraic equations are then solved at each time step with a tridiagonal matrix algorithm written in C. Iterations at each time step proceed until the non-dimensional residual error reduces to less than 10^-6.

Under a charge process, molten salt is supplied to the thermocline liquid heel at 600 °C. A portion of this salt then enters the underling porous bed, as explained in the next section. Cold liquid exits the bottom of the tank, and is solved for with an outflow boundary condition. In the discharge process, the salt reverses direction and enters the bottom of the bed at 300 °C. An outflow condition is again used to solve the corresponding exit of hot salt from the top of the porous bed into the liquid heel. Thermal diffusion between the porous bed and liquid heel is represented with a Dirichlet boundary condition informed by the instantaneous heel temperature, as discussed in the next section. As previously stated, the tank top and side walls are assumed to be well-insulated and adiabatic. For simplicity, the bottom of the porous region is also assumed to be adiabatic.

2.2. Liquid heel

Variations in molten-salt density with temperature generate the potential for dryout of the thermocline porous bed. Dryout must be avoided during storage operations as it would reduce the available energy storage capacity of the granular bed and may also inhibit extraction of hot molten salt from the tank. The liquid heel is therefore maintained at the top of the thermocline tank to prevent dryout of the underlying porous region. In reality, the sigmoid temperature profile along the height of the porous region will extend into this additional volume when the tank approaches a fully-discharged state. However, the height of the heel is not fixed and varies in response to the internal energy content of the tank, prohibiting straightforward analysis with a finite-volume approach. As a conservation approximation, the liquid heel is instead assumed to be an isothermal mass. The mass and energy of the heel are known at each time step as an outcome of the porous region model and surrounding CSP component models, discussed in later sections. The mean temperature of the heel is then calculated from the molten-salt specific heat:

\[ T_{\text{heel}} = T_c + \frac{E_{\text{heel}}}{M_{\text{heel}} C_p^i} \]  

(13)

This heel temperature informs not only energy transport with the underlying porous region but also represents the temperature of salt available for steam generation in the CSP plant power block.

2.3. Model validation

The accuracy of the thermocline tank model is verified by comparing predicted results for a 2.3 MWth molten-salt tank constructed by Sandia National Laboratories against experimental measurements [1]. The tank measured 6.1 m in height and 3 m in diameter, filled with a mixture of quartzite rock and silica sand to a bed height of 5.2 m. The bed porosity was reported to be 0.22. The measured temperature distribution in the tank during a 2-h discharge process is plotted in Fig. 2. The authors did not report a molten-salt flow rate or an initial temperature condition, which are needed inputs to a simulation of the tank. However, the heat-exchange region plotted in Fig. 2 is observed to travel up the thermocline tank at a rate of 2 m per hour. Using Eq. (11), this travel rate for the heat-exchange region corresponds to cold molten salt entering the porous bed at a velocity of 0.436 mm/s. A linear curve is then fit to the earliest measured temperature profile plotted in Fig. 2 to provide an initial temperature condition.

With this estimated inlet velocity and initial temperature profile, the tank discharge is simulated, and the predicted molten-salt temperatures are included in Fig. 2 for comparison with the experimental data. This simulation is performed both with the established CFD model developed in a prior study [3] and with the
reduced-order finite-volume model described in the sections above. The internal filler is approximated as a bed of quartzite rock with an effective diameter of 1.5 cm. The reduced-order model is discretized with an axial cell length (Δx) of 2.2 cm and a time step (Δt) of 3 s. Temperature results with a finer cell length and time step of 1.1 cm and 2 s, respectively, agreed with the coarser discretization to within 0.3% and verified grid convergence. The molten-salt temperature results for both CFD and reduced-order thermocline modeling approaches are included in Fig. 2. The instantaneous temperature profiles are seen to exhibit good agreement with the reported data throughout the entire 2-h discharge operation. Previously stated, temperature in each solid rock is assumed to be homogeneous (i.e., a lumped capacitance). The validity of this assumption is indicated by the Biot number of the quartzite rock:

\[ \text{Bi} = \frac{\text{Nu}}{36(1 - c)} \frac{k_i}{k_r} \]  

During the 2-h discharge, the rock exhibits a maximum Biot number of 0.139. While this value exceeds the conventional limit of 0.1 for lumped capacitance, it should be noted that the local thermal non-equilibrium between molten salt and quartzite is on the order of 1 K. Given that the overall temperature span of the thermocline tank is greater than 100 K, lumped capacitance is an acceptable assumption for the solid region.

It should be also noted that simulation with the reduced-order model is two orders of magnitude faster than the CFD model and did not require the use of a commercial software package. With a validated and low-cost model, study of the thermocline tank is now extended to the system level, in order to investigate the storage performance in response to actual sunlight data and typical solar power plant operation.

3. System-level model development

Development of a system-level power plant model involves the integration of three separate component models – solar collection, energy storage, and power production. The additional components are explained in the following; all component models are sized to operate together as a 100 MW \( p \) power tower plant. The current study assumes no storage bypass, so that all heat and mass transfer between solar collection and power production occurs through the thermocline tank.

3.1. Steam Rankine cycle

As previously mentioned, existing CSP plants achieve power production with a traditional steam Rankine cycle. Hot molten salt generates the necessary superheated steam through a series of heat exchangers (preheater, evaporator, and superheater). In the current study, the steam then travels through a Rankine cycle composed of a non-reheat turbine and a single open feedwater heater for deaeration of the working fluid. The design, illustrated in Fig. 3, is taken from the power block operated at the Solar Two power tower plant [14].

At nameplate or rated conditions, superheated steam enters the turbine at a temperature and pressure of 538 °C and 125 bar (12.5 MPa), respectively (state 1). A portion of the steam (\( y \)) exits the first turbine stage and is sent to the feedwater heater at an intermediate pressure while the remaining steam enters a second turbine stage (state 2). The steam exiting this turbine (state 3) is condensed across the vapor dome at 0.1 bar (10 kPa) and exits the condenser as saturated liquid (state 4). This saturated liquid is then pumped into the feedwater heater (state 5) and mixes with the first turbine stage exhaust. The mixture exits the feedwater heater as saturated liquid (state 6) and is again pumped to 125 bar (state 7). The water then enters the molten-salt heat exchangers and returns to the turbine inlet state as superheated steam. Pressure drops across the various heat exchanger elements are assumed to be negligible. Fig. 4 shows the corresponding temperature-entropy diagram for the rated cycle operation. The turbine and pump machinery are both assumed to exhibit an isentropic efficiency of 0.9 at rated load, resulting in a gross first-law cycle efficiency of 0.4116. Parasitic power consumption within the solar plant requires an overdesign of the power block, fixed at 10.3% for the current study [15]. Therefore, a desired net work output of 100 MW \( p \) requires a gross output of 111.5 MW \( p \) and a corresponding heat input of 270.9 MW for steam generation.

In addition to the rated performance, the combination of the Rankine cycle with a molten-salt thermocline tank also allows for derated operation in response to any salt delivered from the tank at temperatures below the hot design limit of 600 °C. This reduction in exergy is carried through the corresponding steam generation and reduces the turbine inlet temperature. Power production is sustained so long as the thermodynamic cycle adjusts in response to the decrease in steam quality. Known as sliding-pressure operation, the cycle mass flow rates and pressures are both lowered to accommodate the reduced turbine temperature in this mode of operation. The pressure drop across each of the turbine stages exhibits the following relationship with variable mass flow rate [16]:

\[ \frac{\dot{m}_2}{\dot{m}_0} = \frac{p_2^2 - p_2^0}{p_{1,0}^2 - p_{2,0}^2} \]

where \( p_{1,0} \) and \( p_{2,0} \) are the turbine pressures at rated conditions. The isentropic efficiencies of the turbine and pump machinery are also influenced by off-peak performance. Spelling et al. [17] characterized the derated turbine efficiency as a function of turbine speed and enthalpy change:

\[ \eta_t = \eta_{t,0} - 2 \left( \frac{N}{N_0} \sqrt{\frac{\Delta h_{i,0}}{\Delta h_t} - 1} \right)^2 \]

![Fig. 2. Temperature response of a 2.3 MW \( h \), molten-salt thermocline tank undergoing discharge. Numerical simulation is performed with two separate approaches: detailed computational fluid dynamics simulation, and a reduced-order finite volume method. Experimental temperature data reported for the tank [1] are also plotted for model validation.](image-url)
For the current study, both turbine stages are assumed to be constant speed. For pump performance, Lippke [16] reported the following relationship between efficiency and mass flow rate:

\[
\frac{\eta_p}{\eta_{p,0}} = \left( \frac{\dot{m}}{\dot{m}_0} \right)^2
\]

Additional assumptions are necessary to solve the remaining cycle state points for derated operation. The condenser pressure is fixed at 0.1 bar (10 kPa) for all cycle conditions. The outflows of the condenser and feedwater heater are always at saturated liquid conditions. The amount of superheat at the turbine inlet is fixed at 210 K. The preheater also maintains a fixed inlet temperature of 230°C via recirculation of saturated liquid (x = 0) from the evaporator. The derated cycle operation is limited to 30% of the rated gross output, or 33 MWe. The steam turbine inlet temperature associated with this minimum derated condition is 463°C and the corresponding temperature-entropy diagram is included in Fig. 4.

3.2. Steam generators

As stated in the previous section, generation of steam with hot molten salt occurs by means of three heat exchangers: a preheater, evaporator, and superheater. At design conditions, molten salt enters the superheater at 600°C and exits the preheater at 300°C. Water enters the preheater at 230°C, converts to steam at 328°C, and exits the superheater at 538°C. The overall heat transfer coefficients for these heat exchangers are taken from the Solar Two power block [14] and are listed in Table 1. The individual thermal power required for each component is determined from the water vapor dome, and is also included in Table 1. The design surface area for the preheater and superheater is determined using the NTU method. Discussion of these methods is provided in [18]. Fig. 5 shows the temperature response of the molten salt and steam inside each of the heat exchangers as a function of the available surface area.

For derated operation at reduced temperatures, the overall heat transfer coefficient for each heat exchanger becomes a function of the adjusted molten-salt and steam mass flow rates [19]:

\[
\frac{U}{U_0} = \left( \frac{\dot{m}_t}{\dot{m}_{t,0}} \right)^{0.8} \left( \frac{\dot{m}_{\text{water}}}{\dot{m}_{\text{water},0}} \right)^{0.8} \left( \frac{\dot{m}_{t,0}^0 + \dot{m}_{\text{water},0}^0}{\dot{m}_{t,0} + \dot{m}_{\text{water},0}} \right)
\]

The plant model also allows molten salt exiting the preheater at 300°C to recirculate upstream of both the superheater and the evaporator to prevent flow of any saturated mixture outside the evaporator. A plot of the temperature response for 30% derated turbine output is included in Fig. 5. The hot molten-salt temperature necessary for this minimum output is 473°C; thus any molten salt below this temperature is not utilizable for power production and will not be discharged from the thermocline tank. It should also be noted that the required preheater surface area must decrease

<table>
<thead>
<tr>
<th>Heat exchanger</th>
<th>Thermal power, MW</th>
<th>( U, \text{W/m}^2\text{-K} )</th>
<th>Area, m²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preheater</td>
<td>57.34</td>
<td>1940</td>
<td>580.2</td>
</tr>
<tr>
<td>Evaporator</td>
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<td>1392</td>
<td>1042</td>
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<tr>
<td>Superheater</td>
<td>85.12</td>
<td>911</td>
<td>849.8</td>
</tr>
</tbody>
</table>
to sustain the desired exit salt temperature of 300 °C during derated operation. This variable area could be implemented in practice with a shell and tube heat exchanger that includes a tubing manifold. For derated operation, valves in the manifold close a select number of tubes within the heat exchanger and reduce the surface area available for convection.

For combination with the thermocline tank model, the heat exchanger and Rankine cycle models are simplified with polynomial expressions determined from linear regression. These expressions are algebraic relationships between the molten-salt hot supply temperature, molten-salt flow rate in the steam generators, and the gross turbine output power, \( W \) (when salt available from the thermocline tank is above 473 °C). The polynomial curve fits obtained from linear regression are listed below, and are specific to the current problem statement:

\[
\frac{W}{W_0} = -1.706(\theta_{\text{heel}})^3 + 4.406(\theta_{\text{heel}})^2 - 2.031(\theta_{\text{heel}}) + 0.3307
\]

\[
\frac{m_{\text{HX}}}{m_{\text{HX,0}}} = -0.5976(\theta_{\text{heel}})^3 + 0.399(\theta_{\text{heel}})^2 + 1.431(\theta_{\text{heel}}) + 0.2325
\]

The temperature of the molten-salt liquid heel inside the thermocline tank (from which hot salt is delivered to the steam generators) therefore determines both the gross turbine output power and required mass flow rate of molten salt in the power block.

Prior to any daily turbine output being achieved, both the steam generators and the turbine must be conditioned for power production through a multistage process known as startup. This includes warming of the heat exchangers, synchronization of the turbine with the generator, and ramp-up to rated gross output. During the heat exchanger warming and turbine synchronization stage, the thermocline tank supplies hot molten salt to the power block in an amount equivalent to the minimum thermal input (30% load), but with no work output. After synchronization is complete, the turbine initiates power production with a linear ramp-up to rated operation.

The required time intervals for these actions is dependent on the initial turbine temperature, which is itself a function of the length of time since the previous shutdown [20]. For simplicity, this temperature is classified under three states – hot, warm, and cold. The turbine is designated as hot for up to 12 h after a shutdown, after which it degrades to a warm condition. After 72 h of shutdown, the turbine further degrades to a cold condition. Table 2 lists the process times for each turbine temperature state.

### 3.3. Solar collection

For the current study, concentrating and harvesting of direct sunlight is assumed to be performed with a central receiver or power tower design. A surrounding field of dual-axis heliostats follows the position of the sun and reflects the direct normal irradiance (DNI) onto an elevated receiver. Molten salt enters the receiver at 300 °C and exits at 600 °C. The corresponding mass flow rate of molten salt is then a function of the power incident on the receiver. In reality, some fluctuation in the exit temperature does result from the lag in the adjustment of the mass flow rate with varying DNI. However, these events were brief due to a combination of temperature feed-back control and irradiance feed-forward control [14] and are omitted from the present system study.

Both the heliostat field and solar receiver are sized with DEL-SOL [15], a power tower design tool developed by Sandia National Laboratories. For a defined solar multiple and receiver shape, DEL-SOL solves for the optimum heliostat field and then computes the corresponding solar collection efficiency as a function of solar position. Solar multiple is the ratio of sunlight collected at noon on summer solstice relative to the nameplate thermal input to the Rankine cycle and is fixed to 2.3 for the current study. The thermal rating of the solar receiver, 623 MWt, is the product of this multiple and the Rankine cycle heat input at rated load. The corresponding heliostat field includes 1,170,000 m² of reflector area surrounding a tower of height 194.7 m. The solar receiver atop this tower is an external cylinder design with a diameter of 21 m and a height of 18 m. Sunlight data for the plant simulation are taken from measurements near Barstow, CA. Included in this dataset are DNI measurements at 15-min intervals from January 1 to December 31, 1977. This particular dataset was selected for its excellent annual insolation (2700 kW ht/m²), high granularity, and prior application in other power tower studies [20]. The heat collected by the solar receiver in response to the heliostat field and meteorological sunlight data is determined with SOLERGY, a power tower performance model generated by Sandia National Laboratories [21]. At each 15-min interval, SOLERGY calculates the current solar collection efficiency and then outputs the corresponding power absorbed by the molten salt traveling inside the solar receiver. This receiver performance is modeled for the entire year of operation, and is assumed to be independent of the thermocline tank and power block systems. Furthermore, the mass flow rate in the solar receiver is assumed to vary in response to the collected power such that the exiting salt temperature is maintained at 600 °C:

\[
\dot{m}_{\text{rec}} = \frac{P_{\text{rec}}}{C_p(\bar{T}_h - \bar{T}_{\text{rec,in}})}
\]

<table>
<thead>
<tr>
<th>Table 2</th>
<th>Power block startup times for different turbine temperature states [20].</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hours after shutdown</td>
<td>Turbine temperature</td>
</tr>
<tr>
<td>&lt;12</td>
<td>Hot</td>
</tr>
<tr>
<td>12–72</td>
<td>Warm</td>
</tr>
<tr>
<td>&gt;72</td>
<td>Cold</td>
</tr>
</tbody>
</table>
3.4. Model integration

In the current study, the molten-salt thermocline tank is desired to provide the power tower plant with 6 h of thermal energy storage. The maximum energy capacity of the tank should clearly exceed this condition to accommodate simultaneous containment of salt at cold and transitional temperatures. Sizing of the storage system is informed by a previous design study of thermocline tanks published by the Electric Power Research Institute [22], which applied an approximate overdesign of 40% for the tank volume. The study also concluded that the molten-salt liquid level should not exceed 39 feet (11.89 m) to stay within the maximum bearing capacity of the soil with a typical foundation. The height of the model quartzite bed is therefore fixed to 11 m to provide additional volume for the liquid heel above the bed. With the given energy densities of the molten salt and quartzite rock, a thermocline tank diameter of 36.27 m is required to satisfy the requisite energy capacity and volumetric overdesign. The effective diameter of the quartzite rock granules inside the tank is fixed to 1 cm [23].

Integrating the thermocline tank model with the additional component models previously described generates a system-level model of a 100 MWt power tower plant. The individual models interact at the system level as follows. During daylight hours, molten salt picks up solar radiation incident on the receiver and is delivered to the thermocline tank heel. The amount of heat input available at each time step is obtained from the SOLERGY receiver analysis. When the thermocline tank contains enough energy to sustain 2 h of steam generation in the heat exchangers, hot salt is sent to the power block to initiate turbine startup. After startup is complete, the turbine is set for rated power production. Cold salt exiting the power block either returns to the solar receiver or to the bottom of the tank, as dictated by mass balance in the solar collection loop.

It is again noted that no provision for a bypass loop is included between the solar receiver and the power block, and all heat and mass transport in the power plant is routed through the thermocline tank. The thermocline tank operating condition (charge, discharge, or standby) and corresponding salt flow direction is therefore dependent on the immediate disparity in molten-salt mass flow rate between the power block (Eq. (20)) and the solar receiver (Eq. (21)). For example, when the receiver provides hot salt at a faster rate than is necessary in the power block, the thermocline tank is charged with the excess. Conversely, when the power block requires more flow than the amount provided by the receiver, the tank undergoes a discharge to make up the difference. A standby condition with stagnant molten salt (i.e., no flow inside the porous bed) occurs when the discharging tank is depleted of all usable energy.

For prolonged charge processes, the salt exiting the bottom of the thermocline tank will begin to increase in temperature as the transitional heat-exchange region reaches the tank floor. When this warmer salt enters the solar receiver, the receiver mass flow rate increases to maintain the exit hot temperature at 600 °C, governed by Eq. (21). However, cold salt exiting the bottom of the thermocline tank is limited to a maximum allowable temperature of 400 °C to prevent overheating of the storage system. Above this temperature, the thermocline tank is declared to be at energy capacity and transitions to a forced standby condition. With no more available storage, the solar receiver can only collect enough energy to satisfy the Rankine cycle steam generation. Heliostats are defocused away from the receiver and some amount of sunlight available for collection must be forgone: this amount of energy is known as thermal energy discard. The forced tank standby persists until the solar receiver power output decays near sunset and the energy-saturated tank can then be discharged to sustain the rated power production.

Under ideal clear sky conditions on a given day, the thermocline tank would energize to its capacity, go into standby, and finally discharge near sunset following shutdown of the solar receiver. In reality, random cloud transients will lead to sporadic DNI losses during daylight hours. Therefore additional care must be taken in the operation of the thermocline tank to avoid chaotic flow direction changes and consequent wear on the turbine. In the operation considered in the current study, dispatch of hot molten salt from the thermocline tank to the power block is prohibited until the turbine is guaranteed to operate for at least 2 h. Prior to turbine startup, the system model checks both the energy content of the tank as well as receiver performance in the immediate future (already known from the SOLERGY solution) to ensure that this condition on the turbine is satisfied. The authors assume that in practice, plant operators are capable of making similar near-term receiver predictions from weather forecasts. As a result, rapid on–off toggling of either the thermocline tank or the Rankine cycle is avoided.

4. Results and discussion

4.1. CSP plant performance with and without storage

At the onset of the power plant simulation, the thermocline tank fillerbed and liquid heel are both initialized to the cold molten-salt temperature limit of 300 °C. The fillerbed geometry is discretized with a cell length of 2.2 cm (500 cells) and a time step of 3 s; grid independence at this resolution was already verified with the previous simulation of a small-scale thermocline tank. As stated before, the performance of the heliostat field and solar receiver is first simulated in SOLERGY using a meteorological year of sunlight data reported near Barstow, CA. The amount of power collected by the receiver then serves as an input to the integrated thermocline tank and power block models for each time step of simulation.

The resulting plant simulation provides an entire year of performance data for solar collection, storage, and power production. A subset of these results is provided in Fig. 6, where results are shown for the solar receiver power, energy storage, and gross turbine output for 5 days centered on the summer solstice, June 19–23. The daily plant performance represented in the figure is explained as follows. After sunrise, the heliostat field and solar receiver activate and the collected solar power increases from zero. This initial heat collected is sent to the thermocline tank. When the stored energy inside the tank is sufficient for steam generation, the power block undergoes startup procedures, after which the turbine reaches its rated output. As the day progresses, the collected power increases to the 623 MWt rating of the solar receiver, with the excess energy collected being sent to the thermocline tank. Close to sunset, the receiver power begins to decrease until the solar collection system must shutdown for the night. The thermocline tank is then discharged to sustain turbine output into the night. When the thermocline tank energy nears depletion, colder molten salt is supplied to the steam generators and the turbine transitions to derated output until an eventual shutdown.

The receiver data plotted in Fig. 6 exhibit consistent daily performance, corresponding to minimal cloud influence for the selected days. A cloud transient did occur on day 172 of the year, indicated by noise in the receiver power near sunset and an early turbine shutdown relative to the other days. Also of interest is the repeated step decrease in the receiver power that occurs near sunset for the other days plotted in the figure. This reduction occurs when the solar receiver has collected enough excess thermal energy to saturate the thermocline tank, marked by molten salt exiting the bottom of the thermocline tank at 400 °C. As previously discussed, the tank goes into standby and the solar receiver can
only collect thermal energy for steam generation, deviating from the receiver performance predicted by SOLERGY. This deviation quantifies the amount of thermal energy lost due to the lack of additional storage capacity. It should be noted that an economically optimized plant may have a storage system which discards some energy during the peak of the summer, but is heavily utilized during the rest of the year.

For a seasonal perspective, the plant capacity factor is calculated for each month and plotted in Fig. 7. Capacity factor is the ratio of total turbine output over time to the theoretical maximum corresponding to constant output at rated load:

\[
\text{Capacity factor} = \frac{1}{W_0} \frac{\int W(t)dt}{\int dt}
\]  

(22)

Monthly capacity factor is largest in the summer due to the seasonal variation in DNI available for collection, with a maximum value of 0.696 observed for July. With respect to the entire year, the power tower plant generates a total net output of 465.4 GW h, and exhibits an annual capacity factor of 0.531. The overall solar-to-electric efficiency of the power tower plant is defined as the ratio of the net work output to the theoretical maximum amount of sunlight collected (annual solar resource \( \times \) total heliostat area), and achieves a value of 0.147.

The contribution of the thermocline tank to plant performance is observed by repeating the simulation of the current power tower plant, but without a thermal energy storage system. The corresponding monthly capacity factors without storage are included in Fig. 7. As expected, absence of energy storage results in a significant drop in monthly capacity factor relative to the case with a thermocline tank. Year-long operation without storage reduces the annual capacity factor to 0.273 from 0.531 and the solar-to-electric efficiency to 0.076 from 0.147. The simulated thermocline tank was able to store over 8 h of useable heat during operation, which exceeded the originally desired 6 h of storage. Thus the 40% overdesign for the tank size applied from the EPRI design study is shown to be larger than necessary, under the assumptions of the present work.

4.2. Thermocline tank performance

While the capacity factor reveals the impact of the thermocline tank over time, the usefulness of the thermal energy that passes through the storage subsystem for steam generation is quantified by the storage effectiveness, defined as the ratio of utilizable heat delivered from the tank to the maximum heat available:

\[
\varepsilon_{\text{tank}} = \frac{\int \max(C_p(T_{\text{heel}} - T_c)dt}{\int P_{\text{rec}}dt + E_{\text{inj}}}
\]  

(23)

Utilizable heat refers to the available molten salt at sufficient temperature (exergy) for steam generation. The maximum available heat is the total amount of thermal energy delivered to the tank as hot molten salt from the solar receiver plus the initial energy content inside the tank. The monthly storage effectiveness values are plotted in Fig. 8. The effectiveness remains above 99% throughout the year, indicating that over 99% of thermal energy delivered to the tank from the solar receiver each month is later recovered for steam generation.

The excellent effectiveness of the thermocline tank is attributed to the regular (daily) and consistent use of the stored energy during operation, as indicated by the short time duration of standby periods when flow is stagnant inside the tank. The year-long plant simulation, the tank experienced 615 separate instances of standby, of which 98.2% were less than 24 h in duration. This indicates that the tank was operated either in charge or discharge mode on a daily basis throughout the meteorological year. The benefit of this daily operation is a limited residence time of hot molten salt inside the thermocline tank, mitigating the extent of thermal diffusion between the hot salt and the underlying cold salt. Thus for the diurnal cyclic behavior of thermoclines in solar plants, factors that would be detrimental to maintaining thermal stratification inside the tank and would inhibit storage performance over long-term application were found not to play a significant role over the chosen year with the DNI data for Barstow, CA. The thermocline tank is therefore concluded to be a viable thermal energy storage option for use in a solar power plant under such conditions.
The impact of the thermocline tank on power production is a function of its size and energy storage capacity. As previously discussed, thermal energy discard occurs when the thermocline tank becomes saturated with hot salt and is unable to store additional heat. Fig. 8 includes a plot of thermal energy discarded each month, normalized with respect to the amount of sunlight available for collection. As with the plant capacity factor, thermal energy discard displays a strong seasonal dependence corresponding to the variation of DNI received. Winter months receive the least amount of sunlight and thus do not exhibit saturation of thermocline tank on a regular basis. In contrast, summer months experience frequent saturation and exhibit the largest amount of thermal energy discard. During the year, a total of 223 days experience energy saturation of the thermocline tank. The annual thermal energy discard associated with this saturation and subsequent heliostat defocusing is 176 GW h, or 13.7% of the total energy collected by the solar receiver.

An optimal amount of thermal energy discard likely exists for a given solar power plant and energy storage system. If storage saturation and thermal energy discard occurs on a near-daily basis, the storage volume is likely undersized relative to the solar collection system, and this reduces the potential revenue of the solar plant. On the other hand, if thermal energy discard is never observed, the storage volume may be oversized and carry an excessive capital cost. Further investigation and optimization of the thermocline tank is therefore needed to quantify trade-offs in plant cost and annual revenue as a function of tank size.

The validity of the adiabatic tank wall assumption in the present simulation is assessed by estimating the annual heat loss relative to the total amount of energy delivered to the tank from the solar receiver. The EPRI thermocline tank design study proposed mineral wool insulation ($k = 0.2$ W/m-$K$) at a thickness of 23 in. (0.584 m) for the tank [22]. The annual average temperature and wind speed in Barstow, CA in 1977 were 20.1 °C and 4.94 m/s, respectively. For the maximum tank temperature of 600 °C, this external boundary condition generates an average convection heat loss of 203 kW through the mineral wool. The annual energy loss due to this convection is 1775 MW h, or 0.138% of the total hot energy supplied to the thermocline tank from the solar receiver over the year. Given this very low percentage of expected loss, the original adiabatic tank wall assumption is deemed to be acceptable.

### 4.3. System model comparison

In addition to solar receiver performance, thermal energy storage and power production may also be modeled in SOLERGY. It is of interest to compare the simulated plant output from the current study with predictions from SOLERGY. Table 3 includes the annual outputs of the 100 MW power tower plant as predicted by the current study, along with SOLERGY results for both two-tank and thermocline storage systems of equivalent size. As seen in the table, SOLERGY predicts identical plant performance for either the two-tank and thermocline tank storage options. Comparison of the current study and the SOLERGY simulation also shows reasonable agreement, exhibiting a 2.34% difference in annual net turbine output. This difference may be attributed to the lack of molten-salt temperature control in the thermocline tank sub-model implemented in SOLERGY. In the current study, the temperature of salt leaving the bottom of the tank is limited to 400 °C to avoid compromising the heat-exchange region, but this prevents the tank from reaching its maximum energy capacity. In contrast, SOLERGY does not consider such temperature limits and thus overpredicts the thermal energy storage performance in a thermocline tank. This added capacity manifests as greater power production and explains the somewhat larger annual turbine output in Table 3.

It should be noted that SOLERGY and the current system model both apply a sun-following control, which means the turbine is activated whenever sufficient energy is available from storage. In reality, the economic value of electricity is a function of variable time-of-day sale prices and will influence the choice of when the turbine is operational. An alternative plant control strategy would be to delay power production until the most lucrative hours of the day (e.g., weekday afternoons) in order to maximize the annual revenue. However, delaying power production may then lead to an increased occurrence of storage saturation and related thermal energy discard. This potential trade-off between maximizing power production and maximizing revenue is another area of further investigation.

### 4.4. Thermocline structural stability

Along with long-term thermal reliability, the thermocline tank must also exhibit structural stability in response to the repeated cycling during the charge–discharge cycles with hot and cold salt. The tank is also packed with quartzite rock; such quartz-based materials exhibit a change in crystal structure near 573 °C. As this inversion point and the corresponding volumetric expansion are within the applied molten-salt operating temperature range, heating the tank to the maximum hot temperature may lead to large hoop stresses in the surrounding tank wall. Previous structural models for thermocline tanks [6] did not operate above this critical temperature and may not be applicable. Experimental observation as well as further study of granular mechanics inside the thermocline tank is needed to ensure that the tank wall can sustain this quartzite phase change.

To increase safety, the dual-media thermocline tank concept can also be modified either with lower maximum operating temperatures or by use of alternative filler materials. Filler selection...
for the solid rock calls for both low cost and physical stability under repeated thermal cycling. In addition to quartzite, Pacheco et al. [1] reported successful application of iron ore taconite pellets with molten salt. However, physical property data for taconite are not readily available in the literature and require further study. Additional materials not considered in [1] should also be explored.

5. Conclusions

A numerical model for molten-salt thermocline tank operation has been developed to provide accurate simulation of mass and energy transport at low computing cost and without reliance on commercial CFD software. The thermal model is integrated into a system-level simulation of a 100 MW, power tower plant to assess thermocline tank performance under realistic and long-term operating conditions. Operation of the plant model is informed by a meteorological year of sunlight data recorded near Barstow, CA in 1977. The molten-salt thermocline tank, sized to provide 6 h of thermal energy storage, increased the annual plant capacity factor to 0.531 with excellent year-long storage effectiveness exceeding 99%. This good performance results from the regular and consistent utilization of the stored energy in the tank during year-long plant operation, limiting the residence time of hot salt inside the tank and the corresponding loss of thermal stratification that would result. Comparison of the model developed in this work with the results from SOLERGY showed excellent agreement. Additional study is needed to assess the optimum tank size that balances the solar collection system size with the economic impact of turbine delay on maximum hourly electricity prices.

Even if long-term thermal stability is achieved, structural integrity of the thermocline tank remains a design concern due to the large volumetric expansion of the quartzite rock at elevated molten salt temperatures relative to the surrounding tank wall. Further investigation is needed to determine the maximum safe operating temperatures for quartzite rock and also to identify suitable alternative, non-quartz filler candidate materials.

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